

**B.Sc. Semester - 6 (CBCS) Examination****March/April-2026 (NEW COURSE)****Optimization and Numerical Analysis-2 (Core (New))****Time: 2:30 Hours****Marks: 70****Instructions:**

1. All questions are compulsory.
2. Figures to the right indicate marks.

Que.1(A) Answer any two out of three. (10)

- (1) Solve following L.P.P. using simplex method

Maximize  $Z = 16X_1 + 17X_2 + 10X_3$

Subject to:  $X_1 + X_2 + 4X_3 \leq 2000$

$2X_1 + X_2 + X_3 \leq 3600;$

$X_1 + 2X_2 + 2X_3 \leq 2400;$

$X_1 \leq 30; \quad X_1, X_2, X_3 \geq 0$

- (2) Solve following L.P.P. using simplex method

Maximize  $Z = 3X_1 + 2X_2$

Subject to:  $2X_1 + X_2 \leq 10;$

$X_1 + 3X_2 \leq 6; \quad X_1, X_2 \geq 0$

- (3) Solve following L.P.P. using Graphical method.

Maximize  $Z = 2X_1 + 5X_2$

Subject to:  $X_1 \leq 4;$

$X_2 \leq 3;$

$X_1 + 2X_2 \leq 8; \quad X_1, X_2 \geq 0$

Que.1(B) Answer any one out of two (04)

- (1) Find dual of following L.P.P.

Minimize  $Z = X_1 + X_2 + X_3$

Subject to:  $7X_1 - 8X_2 + 4X_3 = 8;$

$X_1 - 2X_2 \leq 2;$

$4X_2 - X_3 \geq 4; \quad X_1, X_2 \geq 0, X_3 \text{ is unrestricted in sign.}$

- (2) Explain method to find dual of given L.P.P

Que.2(A) Answer any two out of three. (10)

- (1) Explain Vogel's Approximation Method to find initial solution of Transportation Problem.
- (2) Find solution of following Assignment Problem for minimize.

| JOBS | MEN |    |    |    |    |
|------|-----|----|----|----|----|
|      |     | 1  | 2  | 3  | 4  |
|      | A   | 8  | 26 | 17 | 11 |
|      | B   | 13 | 28 | 4  | 26 |
|      | C   | 38 | 19 | 18 | 15 |
|      | D   | 19 | 26 | 24 | 10 |

- (3) Find initial solution of following Transportation Problem using Vogel's Approximation Method minimize.

|        | TO |    |    |    |    | Supply |
|--------|----|----|----|----|----|--------|
|        |    | D1 | D2 | D3 | D4 |        |
|        | F1 | 19 | 30 | 50 | 10 |        |
|        | F2 | 70 | 30 | 40 | 60 |        |
|        | F3 | 40 | 8  | 70 | 20 |        |
| Demand |    | 5  | 8  | 7  | 14 |        |

- Que.2(B) Answer any one out of two (04)
- (1) Explain Hungarian Method to find solution of Assignment Problem.
  - (2) Find initial solution of following Transportation Problem using North West Corner Rule.

|      | TO     |    |    |    |    | Supply |
|------|--------|----|----|----|----|--------|
|      |        | D1 | D2 | D3 | D4 |        |
|      | F1     | 19 | 30 | 50 | 10 |        |
|      | F2     | 70 | 30 | 40 | 60 |        |
| FROM | F3     | 40 | 8  | 70 | 20 | 18     |
|      | Demand | 5  | 8  | 7  | 14 |        |

- Que.3(A) Answer any two out of three. (10)
- (1) Derive Bessel's interpolation formula for central differences.
  - (2) Prove that divided differences are symmetrical in all their arguments.
  - (3) Derive Gauss's forward interpolation formula.
- Que.3(B) Answer any one out of two (04)
- (1) Derive Lagrange's interpolation formula for unequal intervals.
  - (2) Derive relation between divided differences and forward differences.
- Que.4(A) Answer any two out of three. (10)
- (1) Define numerical integration and derive general quadrature formula.
  - (2) Derive Simpson's 1/3 and 3/8 rules.
  - (3) Obtain derivatives using Gregory Newton's backward interpolation formula.
- Que.4(B) Answer any one out of two (04)
- (1) Evaluate  $\int_4^{5.2} \log x \, dx$  by Trapezoidal rule.
  - (2) State and prove Trapezoidal rule.
- Que.5(A) Answer any two out of three. (10)
- (1) Solve  $\frac{dy}{dx} = f(x, y)$ ,  $y(x_0) = y_0$ , by Euler's method.
  - (2) Solve  $\frac{dy}{dx} = f(x, y)$ ,  $y(x_0) = y_0$ , by Milne's predictor – corrector method.
  - (3) Solve  $\frac{dy}{dx} = 3x + y/2$ ;  $y(0) = 1$  find  $y(0.1)$  using Taylor's series method.
- Que.5(B) Answer any one out of two (04)
- (1) Solve  $\frac{dy}{dx} = f(x, y)$ ,  $y(x_0) = y_0$ , by Taylor's method.
  - (2) Let  $\frac{dy}{dx} = 3x + y^2$ ;  $y(0) = 1.2$  find  $y(1.1)$  using Runge's method.

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